

## Worksheet on Barrier Functions: Example 1

$$\begin{aligned} \min_x & (x-3)^2 \\ \text{s.t.} & x \geq 0 \end{aligned}$$

1. Transform the problem into a barrier function form:

$$\begin{aligned} \min_{x \in \mathbb{R}^n} & f(x) \\ \text{s.t.} & c(x) = 0 \\ & x \geq 0 \end{aligned} \quad \longrightarrow \quad \begin{aligned} \min_{x \in \mathbb{R}^n} & f(x) - \mu \sum_{i=1}^n \ln(x_i) \\ \text{s.t.} & c(x) = 0 \end{aligned}$$

2. Verify the optimal barrier function solution at one of the follow values of the barrier term:  $\mu=1$   $\mu=2$   $\mu=5$   $\mu=10$ .

