

Name: \_\_\_\_\_

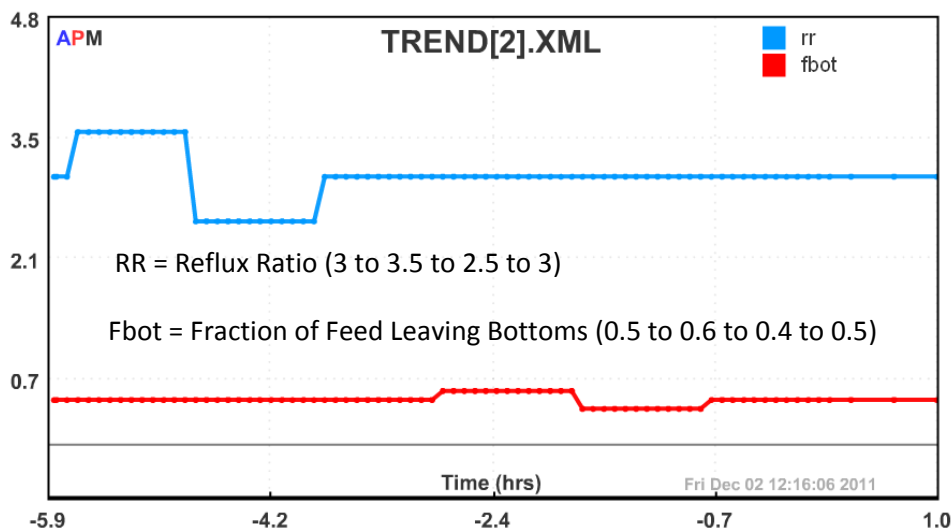
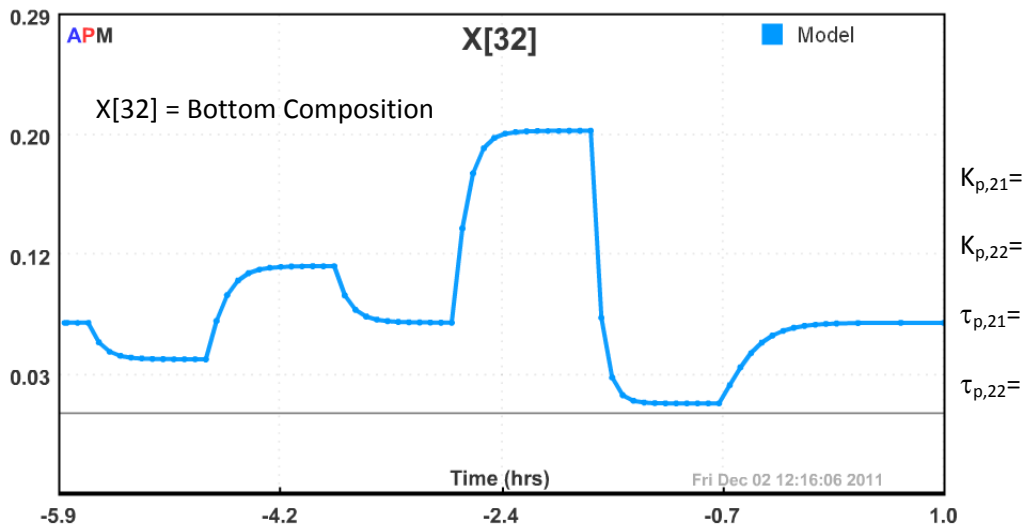
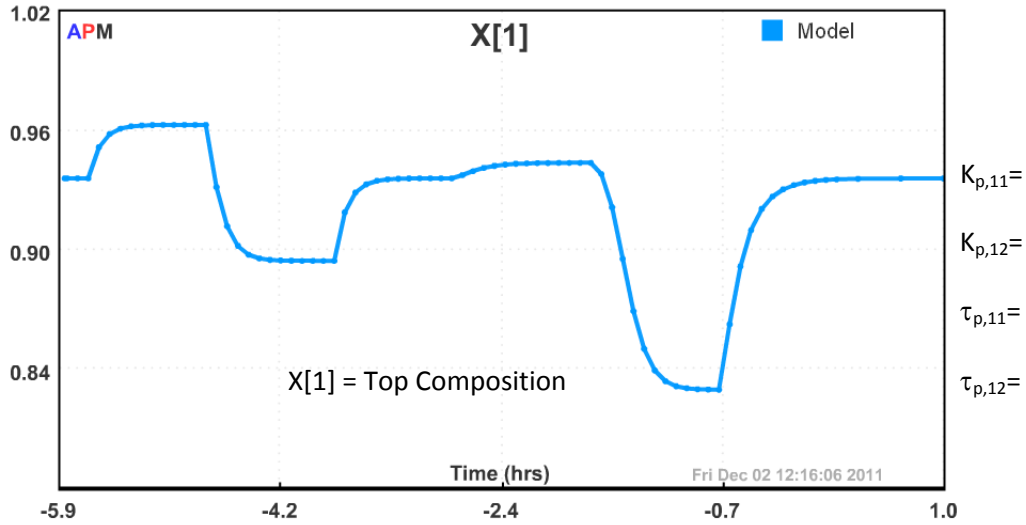
### SP16 - Process Control 436

The purpose of this assignment is to design a control system for a distillation column. A distillation column is typically a highly coupled system that leads to interacting controllers. Techniques from this class that are useful for designing the control system are:

- Empirical model fitting of a Multiple Input Multiple Output (MIMO) System
- Relative Gain Array (RGA) analysis to determine best pairing of Manipulated and Controlled Variables
- Trial Controller with PID Non-interacting controllers
- Trial PID Controllers with Feedforward information from other controllers
- Derivation of First Principles model
- Nonlinear Control (NLC)

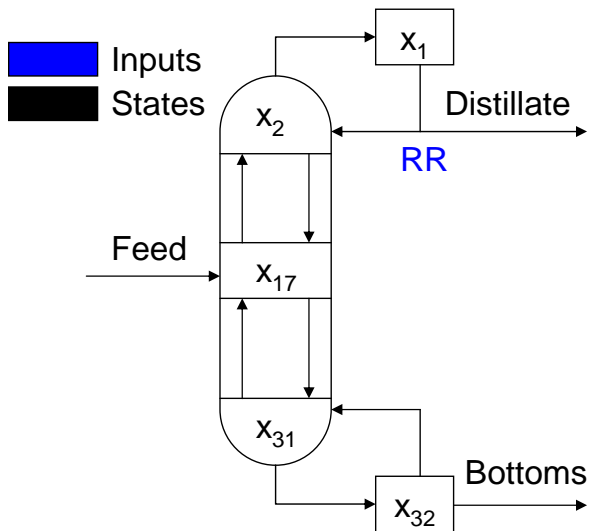
Part a) Calculate transfer functions for the distillation column model response and put model into the form

$$\begin{bmatrix} X[1] \\ X[32] \end{bmatrix} = \begin{bmatrix} \frac{K_{p,11}}{\tau_{p,11}s + 1} & \frac{K_{p,12}}{\tau_{p,12}s + 1} \\ \frac{K_{p,21}}{\tau_{p,21}s + 1} & \frac{K_{p,22}}{\tau_{p,22}s + 1} \end{bmatrix} \begin{bmatrix} RR \\ Fbot \end{bmatrix} =$$



**Part b)** Derive a single tray model for the distillation column:

- Two Components
- Constant Relative Volatility
- Constant Tray Molar Holdup
- Liquid Feed at the Bubble Point
- 30 Trays, Reboiler, and Condenser
- Manipulated Variables
  - RR – Reflux Ratio
  - FBOT – Fraction of Feed Leaving at Bottoms Product
- Controlled Variables
  - $x[1]$  – Light component composition in overhead product
  - $x[32]$  – Light component composition in bottoms product



**Part c)** Using Relative Gain Array (RGA) analysis, suggest best pairing options for the MVs (RR and FBOT) and CVs (X[1] and X[32]). The steady state gains at a nominal operating condition are provided below.

APMonitor		CV(1)	CV(2)	SV(1)	SV(2)	SV(3)	SV(4)	SV(5)	SV(6)	SV(7)	SV(8)
	Sensitivities	ss.x[1]	ss.x[32]	ss.x[2]	ss.x[5]	ss.x[10]	ss.x[15]	ss.x[20]	ss.x[25]	ss.x[30]	ss.x[31]
<b>FV(1)</b>	ss.feed	-4.204E-09	4.204E-09	-5.313E-09	-5.383E-09	-2.321E-09	8.049E-09	5.356E-09	6.675E-09	5.061E-09	4.792E-09
<b>FV(2)</b>	ss.x_feed	0.880362	1.11964	1.30545	2.42762	2.64995	1.80586	2.16519	3.25674	2.00723	1.55214
<b>FV(3)</b>	ss.alpha	0.446683	-0.446683	0.606380	0.889874	0.565205	0.095437	-0.178455	-0.702162	-0.689056	-0.574441
<b>FV(4)</b>	ss.atray	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
<b>FV(5)</b>	ss.acond	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
<b>FV(6)</b>	ss.arih	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
<b>MV(1)</b>	ss.rr	0.068707	-0.068707	0.101883	0.170145	0.121322	0.019434	-0.050178	-0.152264	-0.118547	-0.093852
<b>MV(2)</b>	ss.fbot	0.314140	1.42754	0.465825	0.866247	0.945584	0.644385	1.43757	3.39092	2.48516	1.95664

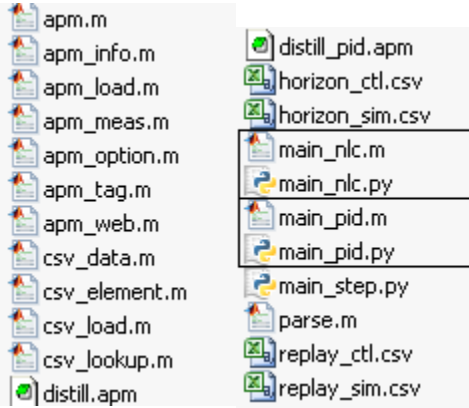
The RGA analysis can be completed by using the gains above or the gains from Part a)

$$\lambda_{11} = \lambda_{22} = \frac{1}{1 - \frac{K_{12}K_{21}}{K_{11}K_{22}}}$$

$$\lambda_{12} = \lambda_{21} = 1 - \lambda_{11}$$

$$\Lambda = \begin{bmatrix} \lambda_{11} & \lambda_{12} \\ \lambda_{21} & \lambda_{22} \end{bmatrix} =$$

**Part d)** Simulate a PID controller for the distillation column using files provided with this assignment (run **main\_pid.py**). Adjust the PI controller tuning parameters to achieve acceptable set point and disturbance tracking. PI controller tuning can be adjusted by opening **distill\_pid.apm** with a text editor and modifying the values of  $K_c_1$ ,  $K_c_2$ ,  $\tau_{ai_1}$ , and  $\tau_{ai_2}$ .

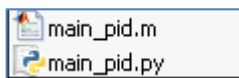


Edit  **distill\_pid.apm** with a text editor to change the PID tuning parameters.

```
! pid tuning parameters for top composition control
kc_1  = 1/0.069  ! ~1/Kp1
taui_1 = 30      ! ~taup1
taud_1 = 0      ! 0
sp_x[1] = 0.935

! pid tuning parameters for bottom composition control
kc_2  = 1/1.42   ! ~1/Kp2
taui_2 = 60     ! ~taup2
taud_2 = 0     ! 0
sp_x[32] = 0.065
```

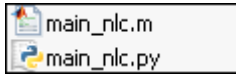
Run PID Control with either MATLAB or Python



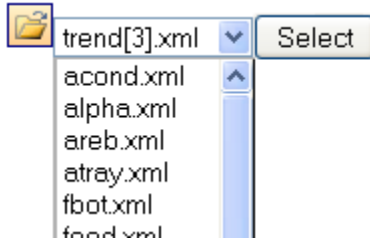
**(Extra):** Adjust the PID equations in **distill\_pid.apm** to make them interacting controllers (i.e. a feedforward element) that accounts for changes in the other controller.

**Part e)** Compare the performance of the PID controller with Nonlinear Control.

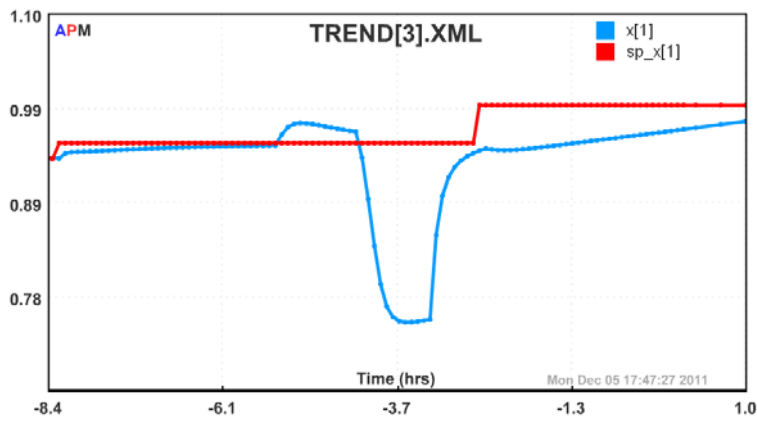
Run Nonlinear Control with either MATLAB (**main\_nlc.m**) or Python (**main\_nlc.py**):



When the web-viewer starts, select custom trends **Trend[3]** or **Trend[4]** to view controller performance.



PID Control Performance for Distillate Composition Control



NLC Control Performance for Distillate Composition Control

