

# ChE 263

## Assignment #5

The assignment is due midnight **before** the beginning of the next class period. Upload completed assignment to Learning Suite.

1. A first order reaction is governed by  $A \rightarrow B$  and has rate

$$\frac{dC_A}{dt} = -kC_A$$

where  $C_A$  is the concentration ( $\text{kmol/m}^3$ ),  $t$  is time, and  $k$  is a rate constant. The initial concentration is  $C_{A0} = 5 \text{ kmol/m}^3$ , and  $k = 1 \text{ s}^{-1}$ .

- a. Solve for  $C_A(t)$  two ways: (1) analytically by separating variables and integrating; (2) using the Explicit Euler method. For the Euler method, evaluate the rate (RHS function) at time  $n$ , then solve the whole equation for values at time  $n+1$ .

$$\frac{dC_A}{dt} \approx \frac{C_{A_{n+1}} - C_{A_n}}{t_{n+1} - t_n} = f(C_{A_n})$$

$$C_{A_{n+1}} = f(C_{A_n})\Delta t + C_{A_n}$$

Plot the two versions of  $C_A(t)$  on the same plot. Label and format the plot including axis labels, and legends, etc. so that you can clearly communicate the solution. Use a time step size of  $\Delta t = 0.5 \text{ s}$  and plot to  $t_{end} = 7 \text{ s}$  (14 steps).

- b. Compare the curves. Why are they different?
- c. Copy the figure and paste as an image in the same document. Change  $\Delta t$  from 0.5 to 1.5. Copy the figure as an image again. Change  $\Delta t$  to 2.1. Observe the three plots that correspond to three different values of  $\Delta t$ .

2. We are performing a chemical reaction as follows:



Product C is desired, but as soon as some C is formed, some B reacts with it to form an undesired product D.

The rate of change of the concentrations of each of the species is given by

$$dA/dt = -k_1 A B$$

$$dB/dt = -k_1 A B - k_2 B C$$

$$dC/dt = k_1 A B - k_2 B C$$

$$dD/dt = k_2 B C$$

(Here, symbols A, B, C, and D denote the species concentrations in mol/L). The initial concentrations are  $A_0=1$ ,  $B_0=1$ ,  $C_0=0$ ,  $D_0=0$ . Also,  $k_1 = 1$  L/mol-s, and  $k_2 = 1.5$  L/mol-s

- Solve** for the concentrations of A, B, C, and D as functions of time. Use a time step size of  $dt=0.2$  s and solve to  $t=3$  s. Also solve for the selectivity defined as  $S = C/(C+D)$  as a function of time. (S is initially undefined, but you can set it equal to 1 at  $t=0$ .) Use Euler's equation applied to each  $d(\text{Species})/dt$  above:  $dy/dt = f(y,z,w,\text{etc.}) \rightarrow y_{n+1} = y_n + \Delta t * f(y_n, z_n, w_n, \text{etc.})$ .
- Plot** the concentrations of A, B, C, D, and S as functions of time on the same plot. Label the axes as "time (s)" and "concentration (mol/L)".
- What is the **final value of the selectivity**? (Color the cell yellow)
- Assuming the values of  $C_0$ ,  $D_0$ ,  $k_1$  and  $k_2$  are fixed, **how can you increase the final value of the selectivity** given the above reactions?