

# Mathcad Summary

## Basics

Toolbars

Equal signs: =, :=, ≐

Subscripts: "." vs "["

Greek letters: ctrl-g

Matrix: ctrl-m

Plot: @

Arrays start at 0, but change with ORIGIN:=1 or whatever

Evaluate: top to bottom and left to right

Units: Always work with K or R, never C, F, be careful when plotting.

Symbolic toolbar, versus symbolic menu

## Integration

Define the function, then use the symbolic integral (calculus toolbar)

$$f(x) := 2x^2 + 1$$

$$\int_0^1 f(x) dx = 1.667$$

## Curve Fitting

### Polynomial

Use functions regress and interp

$$x := (0 \ 1 \ 2 \ 3 \ 4 \ 5)^T$$

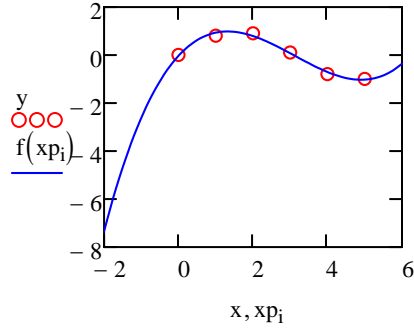
$$y := (0 \ 0.8 \ 0.9 \ 0.1 \ -0.8 \ -1)^T$$

$$i := 0..99$$

$$xp_i := i \cdot \frac{8}{99} - 2$$

$$p3 := \text{regress}(x, y, 3)$$

$$f(xp) := \text{interp}(p3, x, y, xp)$$



## General fit

Use genfit function. Need to include partial derivatives

Fit given x, y data below to function:  $f(x) = a \cdot \exp(-b \cdot x) + c$

$$x := (0 \ 0.41 \ 0.82 \ 1.22 \ 1.63 \ 2.04 \ 2.44 \ 2.86 \ 3.26 \ 3.67)^T$$

$$y := (3.14 \ 2.0 \ 1.29 \ 1.34 \ 0.55 \ 0.77 \ 0.45 \ 0.65 \ 0.29 \ 0.58)^T$$

$$f(x, a, b, c) := a \cdot \exp(-b \cdot x) + c$$

$$\frac{d}{da} f(x, a, b, c) \rightarrow e^{-b \cdot x}$$

$$\frac{d}{db} f(x, a, b, c) \rightarrow -a \cdot x \cdot e^{-b \cdot x}$$

$$\frac{d}{dc} f(x, a, b, c) \rightarrow 1$$

$$g(x, a) := \begin{pmatrix} a_0 \cdot \exp(-a_1 \cdot x) + a_2 \\ e^{-a_1 \cdot x} \\ -a_0 \cdot x \cdot e^{-a_1 \cdot x} \\ 1 \end{pmatrix}$$

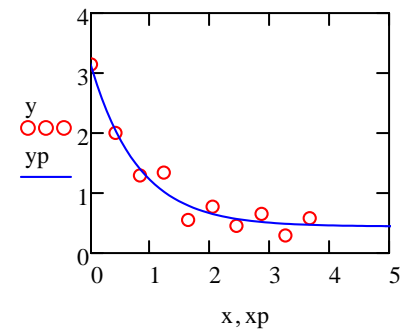
$$ag := \begin{pmatrix} 2 \\ 1 \\ 0.5 \end{pmatrix}$$

$$a := \text{genfit}(x, y, \text{ag}, g) \quad a = \begin{pmatrix} 2.677 \\ 1.251 \\ 0.441 \end{pmatrix}$$

$$i := 0..99$$

$$xp_i := i \cdot \frac{8}{99} - 2$$

$$yp := f(xp, a_0, a_1, a_2)$$



## Interpolation

Use functions `linterp` (for linear interpolation) and `cspline` for cubic splines

Define the given `x`, `y` data points, and the `x_interp` points to interpolate to

$$i := 0..9$$

$$x_i := i \cdot \frac{10}{9}$$

$$y := \cos\left[\frac{-(x)^2}{8}\right]$$

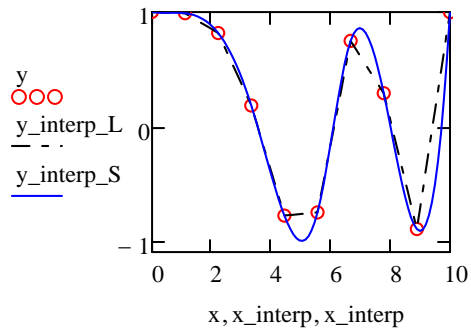
$$j := 0..99$$

$$x\_interp_j := \frac{j \cdot 10}{99}$$

$$y\_interp\_L := \text{linterp}(x, y, x\_interp)$$

$$cs := \text{cspline}(x, y)$$

$$y\_interp\_S := \text{interp}(cs, x, y, x\_interp)$$



## ODE System

Solve functions:  $\frac{dv}{dt} = -9.81 + v^2$

$$\frac{dx}{dt} = v$$

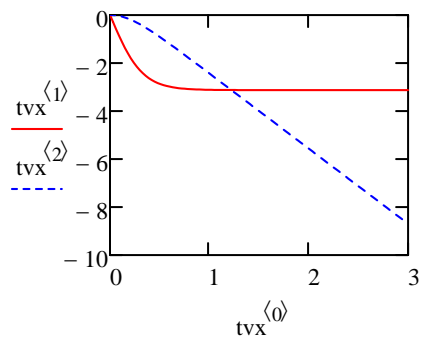
with initial condition  $v0 = 0$   $x0 = 0$

$$y0 := \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

$$D(t, y) := \begin{bmatrix} -9.81 + (y_0)^2 \\ y_0 \end{bmatrix}$$

tstart := 0    tend := 3    npts := 100

tvx := rkfixed(y0, tstart, tend, npts, D)



## System of Nonlinear Equations

Functions: root, polyroots, Given/Find block

Find a solution to the following two equations for y, z

$$y = z^3 - 3z^2 + 5z + 3$$

$$z = z + 10$$

$$y := 1.0$$

$$z := 1.0$$

Given

$$y = z^3 - 3z^2 + 5z + 3$$

$$y = z + 10$$

$$\begin{pmatrix} y \\ z \end{pmatrix} := \text{Find}(y, z)$$

$$y = 12.516$$

$$z = 2.516$$

## System of Linear Equations

Find solution x for system  $Ax=b$

$$A := \begin{pmatrix} 1 & -2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}$$

$$b := \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}$$

$$x := \text{lsolve}(A, b)$$

or

$$x := A^{-1} \cdot b$$

$$x = \begin{pmatrix} -2.875 \\ 0.75 \\ 1.458 \end{pmatrix}$$

